

# DCSC

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F. Stoffelen (TNO), R. Wilson (Durham UK))

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1. **D**<sub>ELFT</sub> **C**<sub>ELEBRATES</sub> **S**<sub>YSTEMS</sub> and **C**<sub>ONTROL</sub>

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2. **D**<sub>O</sub> **C**<sub>RAZY</sub> **S**<sub>TUDY</sub> and **C**<sub>ONTROL</sub>
3. **D**<sub>EALING WITH</sub> **C**<sub>OMPLEXITY BY EXPLOITING</sub> **S**<sub>TRUCTURE IN</sub>  
and **C**<sub>ONTROLLER DESIGN</sub>

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1. What challenges does Complexity offers to Control?

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# Complexity (L. *complexus*)

**Websters:** refers to that which is made up of many elaborately interrelated or **interconnected parts**, so that much study or **knowledge** is needed to understand or to operate it.

# Founding Principle of Control Engineering

The field of control is **built on** the tradition of **linking applications, theory and computation** to develop techniques with rigorous mathematics.

Panel on Future Directions in CDS, 2002

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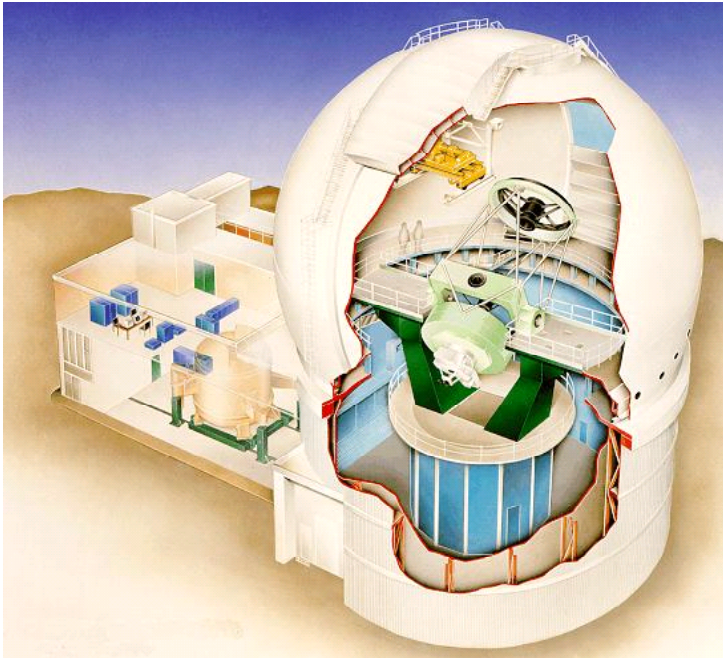
# Probing the Universe

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Astronomical telescopes are essential tools to access the widest and most comprehensive laboratory of all, the universe we live in.

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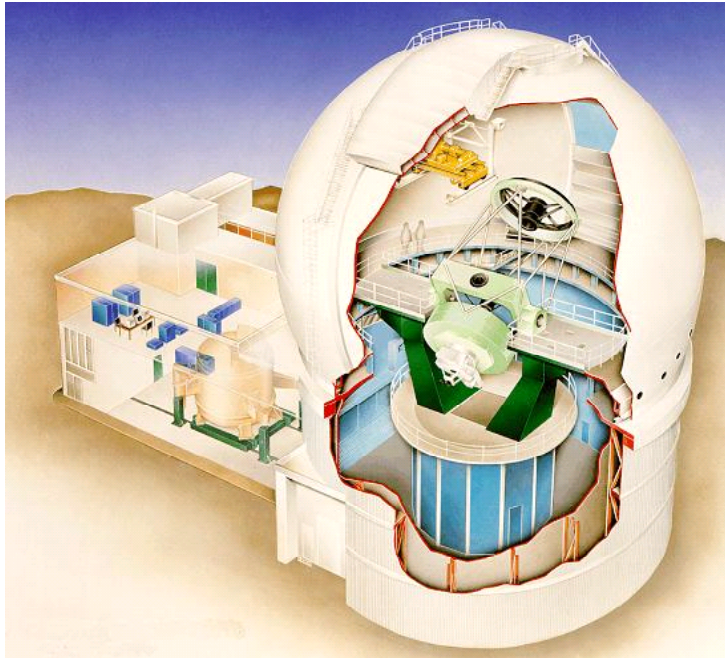
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The William-Herschel Telescope

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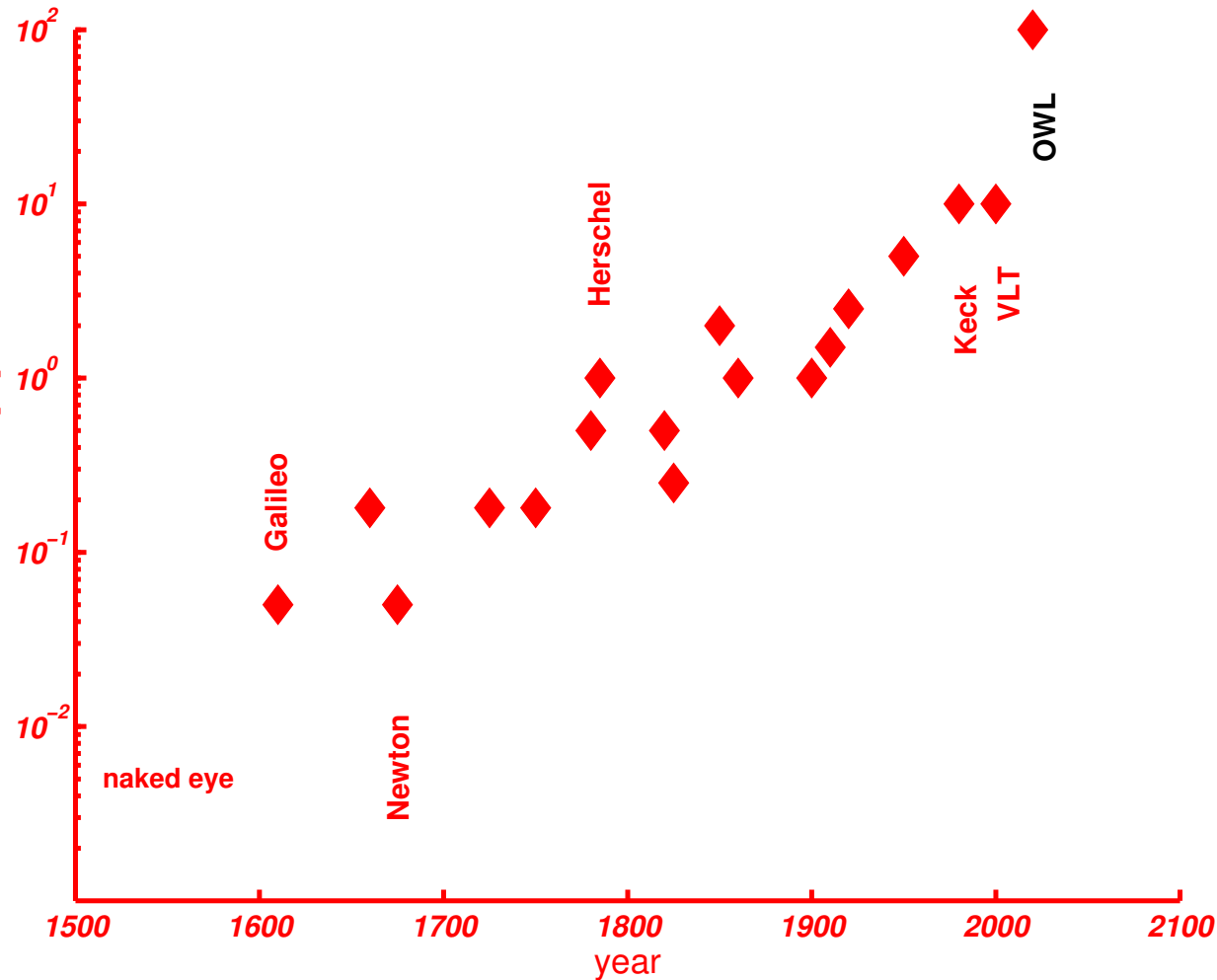
The William-Herschel Telescope

Telescopes enabled new discoveries, like

Quasars, masers, black holes, gravitational arcs, extra-solar planets, gamma-ray bursts, dark matter, dark energy



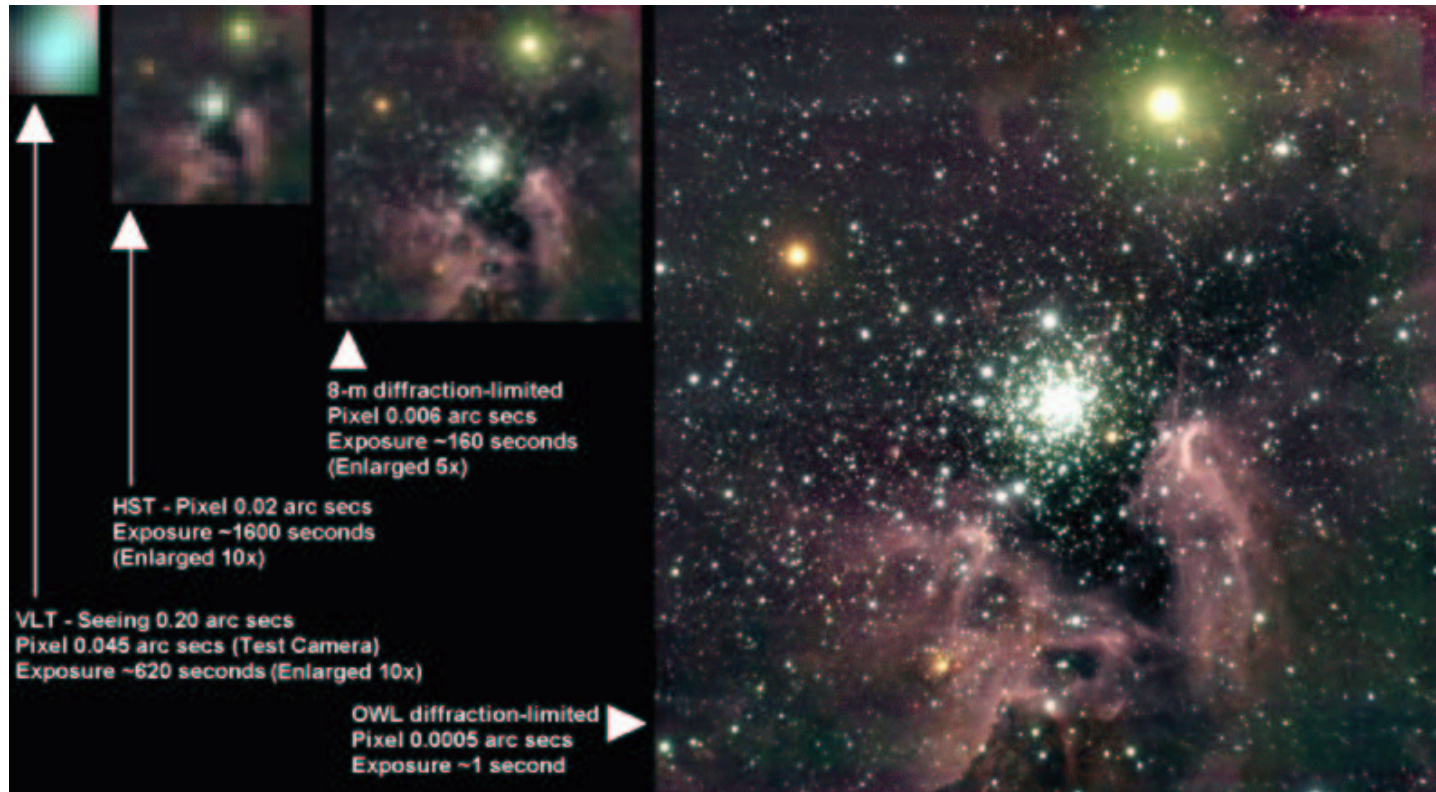
# A Quantum Leap in Telescope Development



Evolution of telescope diameter over time

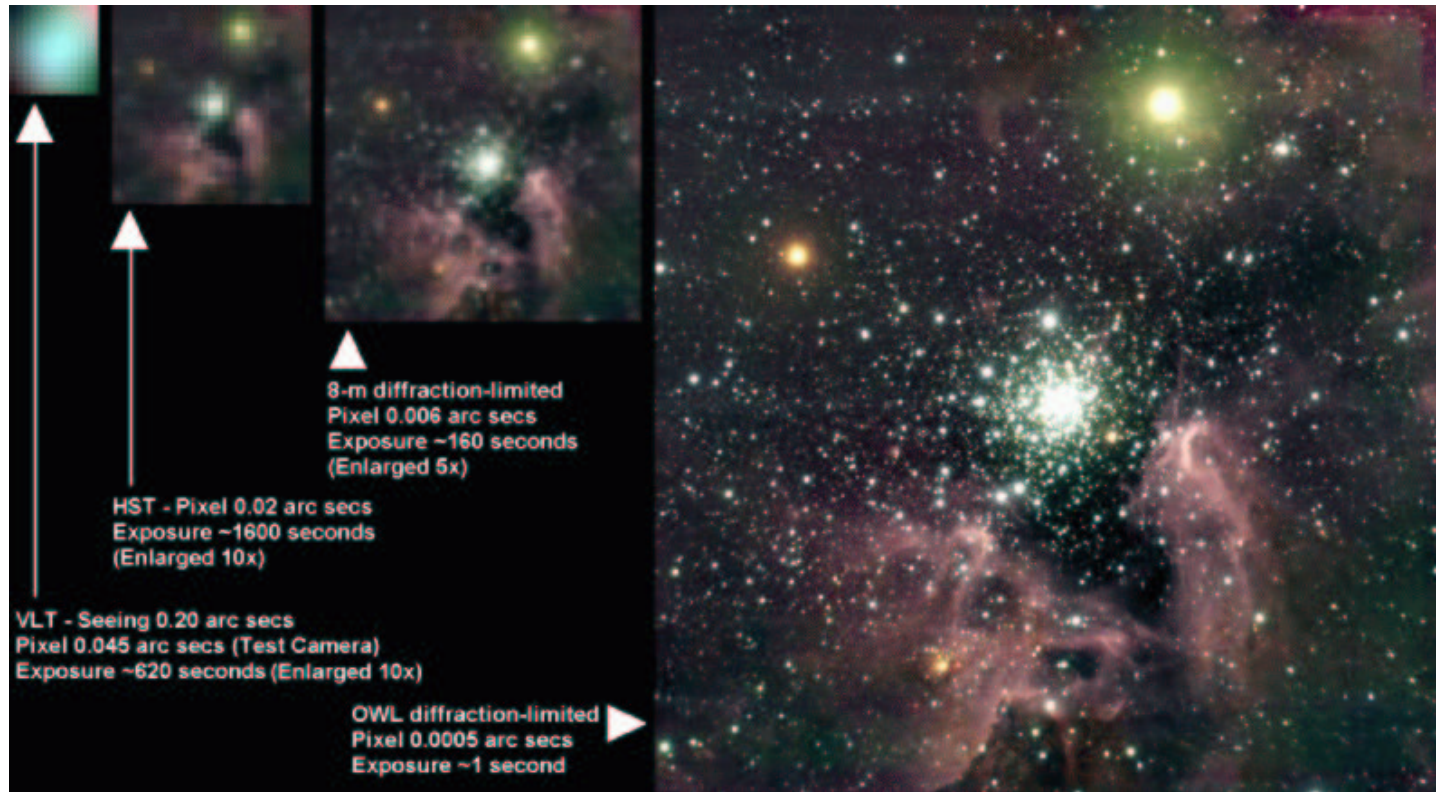
Each new generation of telescopes is designed to answer the questions raised by the previous ones.

# Potential of OWL



Simulated images of the increase of resolution and efficiency with telescope size

# Potential of OWL



Simulated images of the increase of resolution and efficiency with telescope size

**OWL** will make us witness the development of galaxies

# Complexity Issues in Future Telescope Designs

Future Telescope Dimensions will be possible by the **collaboration of distributed** sensores and actuators

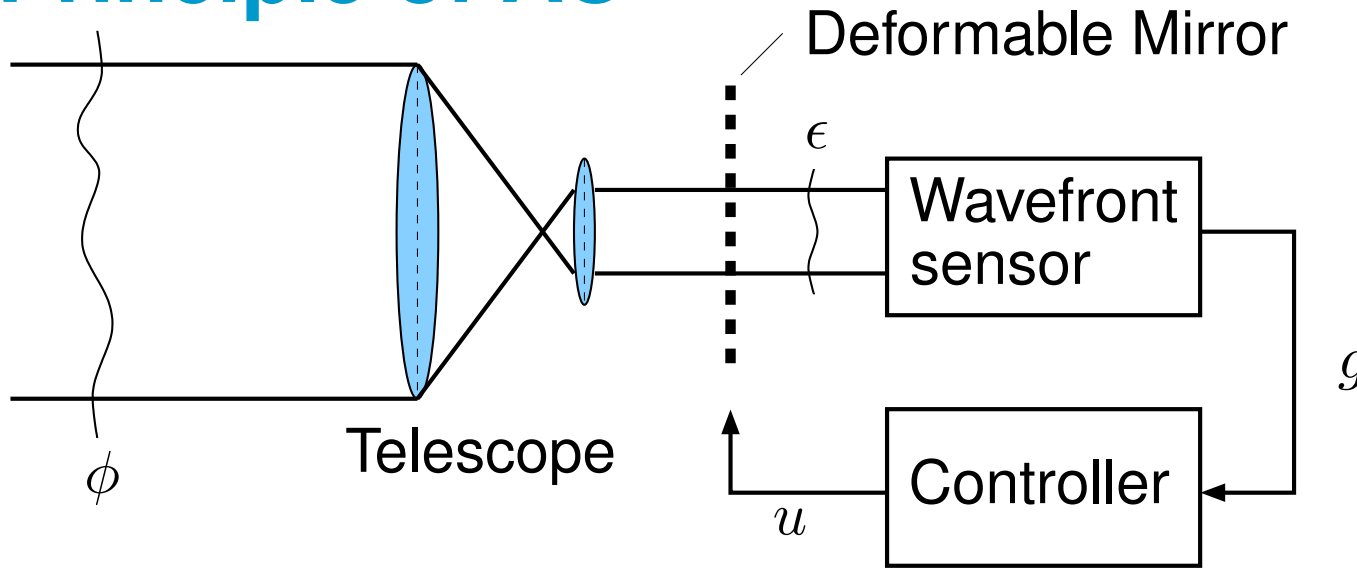
**Example:** A 32 meter telescope may consist of **9000** Deformable Mirror (DM) actuators and **16000** Wavefront Sensors (WFS) subapertures.

[B.L. Ellerbroek, et. al, Applied Optics, 2003]

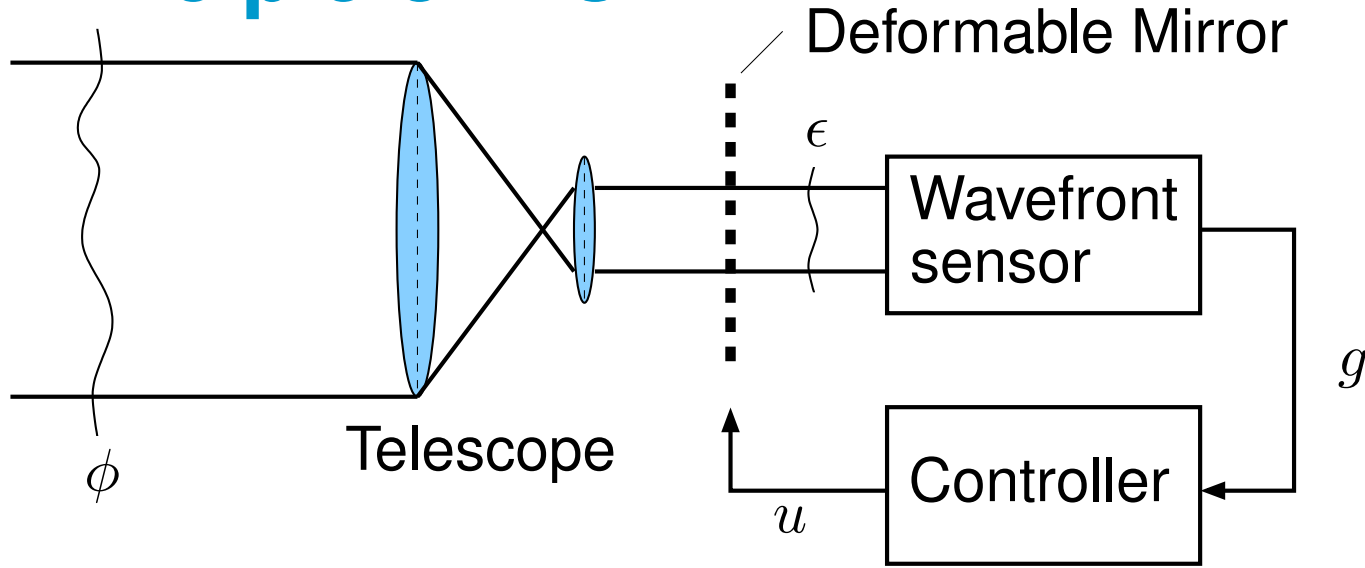
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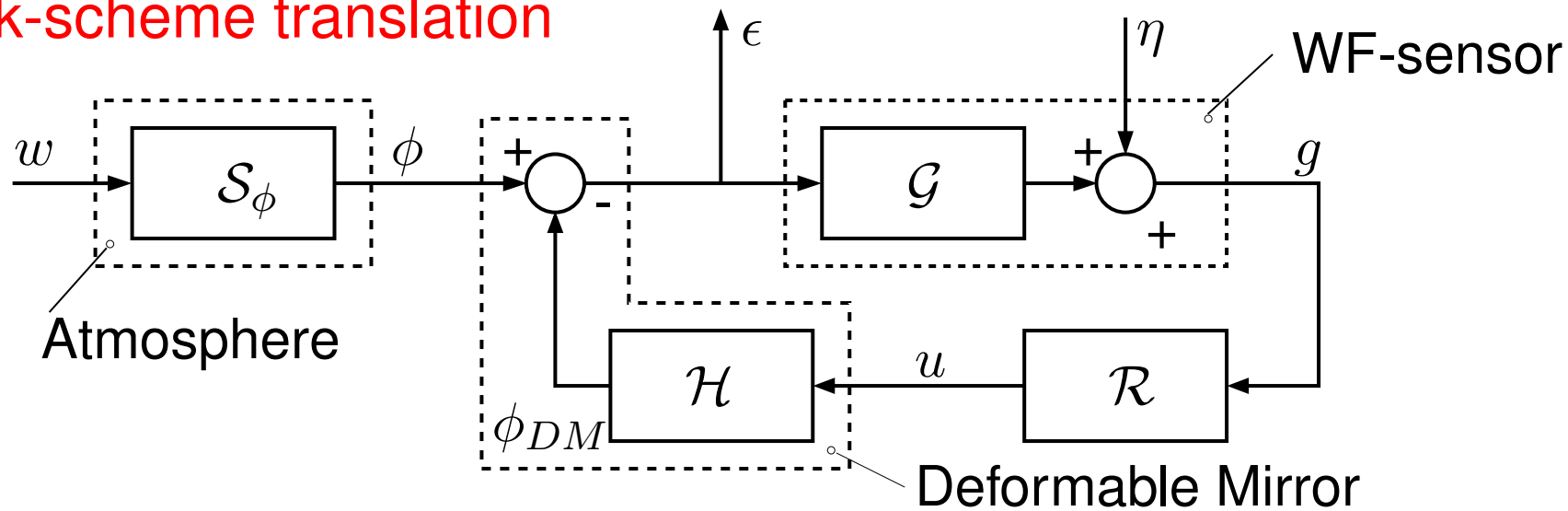
# Principle of AO



# Principle of AO



## Block-scheme translation



# State of the Art in AO

The **standard formulation** to minimize the mean-square residual phase error, i.e.  $\|\epsilon\|_2^2$ , is based on the simplifying assumptions:

1. Only spatial dependency ( $\mathcal{G}$ , etc. are large structured matrices).
2. The WFS measurement vector  $s$  is a linear function of the phase distortion  $\phi$ , whereas  $\phi$  follows the non-rational Kolmogorov power spectrum:

$$\Phi(\kappa) = \frac{0.023}{r_0^{5/3} \kappa^{11/3}}, \quad \begin{array}{l} (\kappa \text{ spatial frequency,} \\ r_0 \text{ Fried coherence length)} \end{array}$$

3. The WFS measurement vector  $s$  is **an open-loop** measurement that is obtained prior to correcting the phase errors

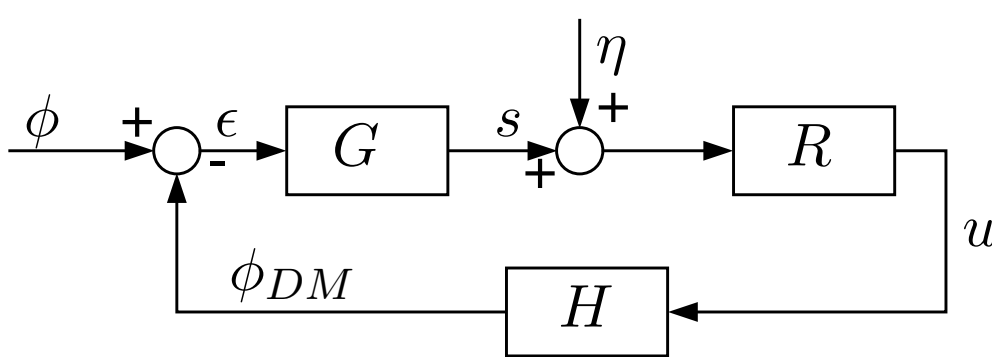
[B.L. Ellerbroek, et. al, Optical Society of Am., 2003]



# State of the Art in AO

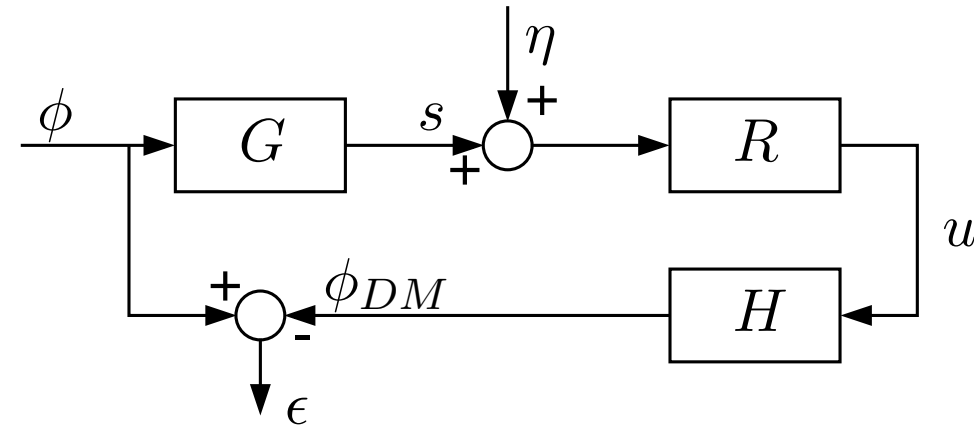
By the standard assumptions, the feedback control problem is “linearized” into a feedforward reconstruction problem.

feedback  $\xrightarrow{\text{Assumptions}}$  feedforward



$$\min_R \|\epsilon\|_2^2$$

?



$$\min_R \|\epsilon\|_2^2$$

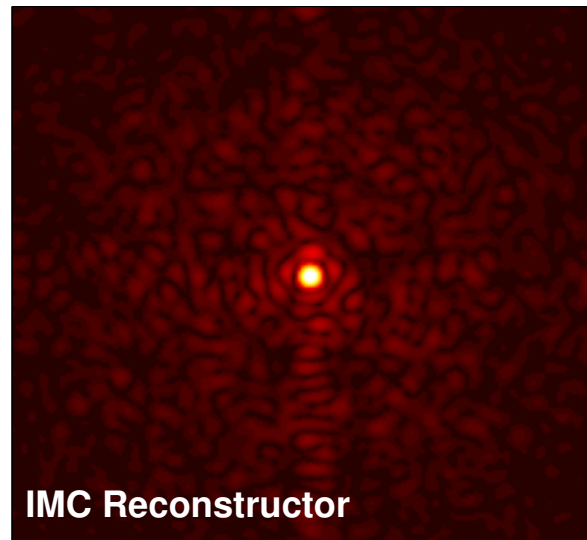
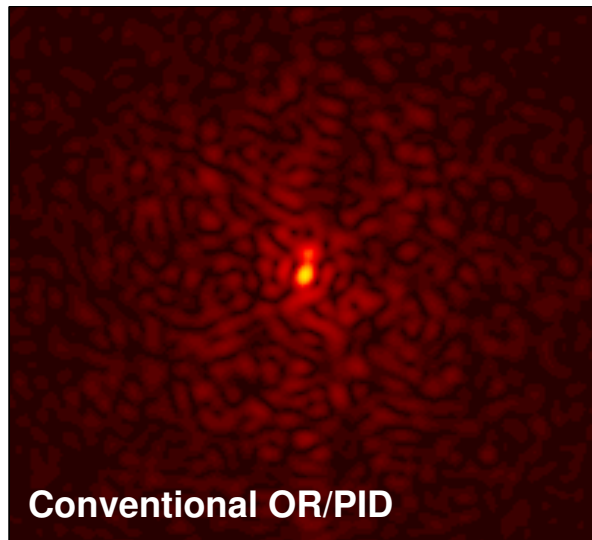
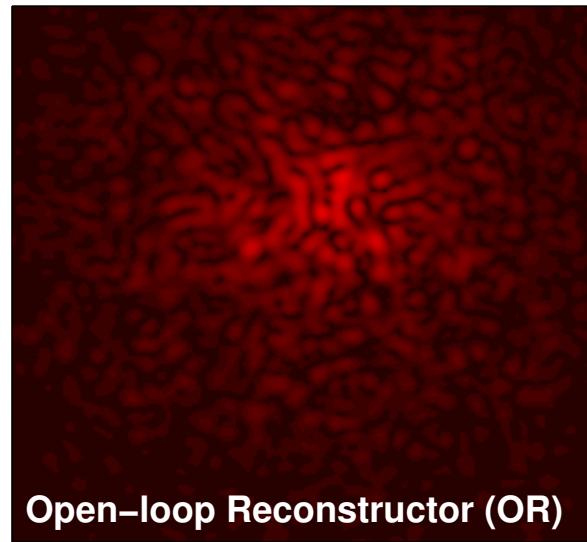
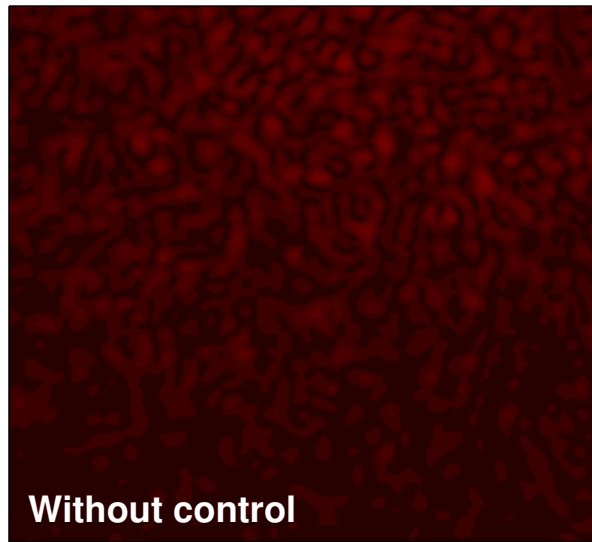
$$\hat{R} = (HH^T)^{-1} H^T C_\phi G^T (GC_\phi G^T + C_n)^{-1}$$

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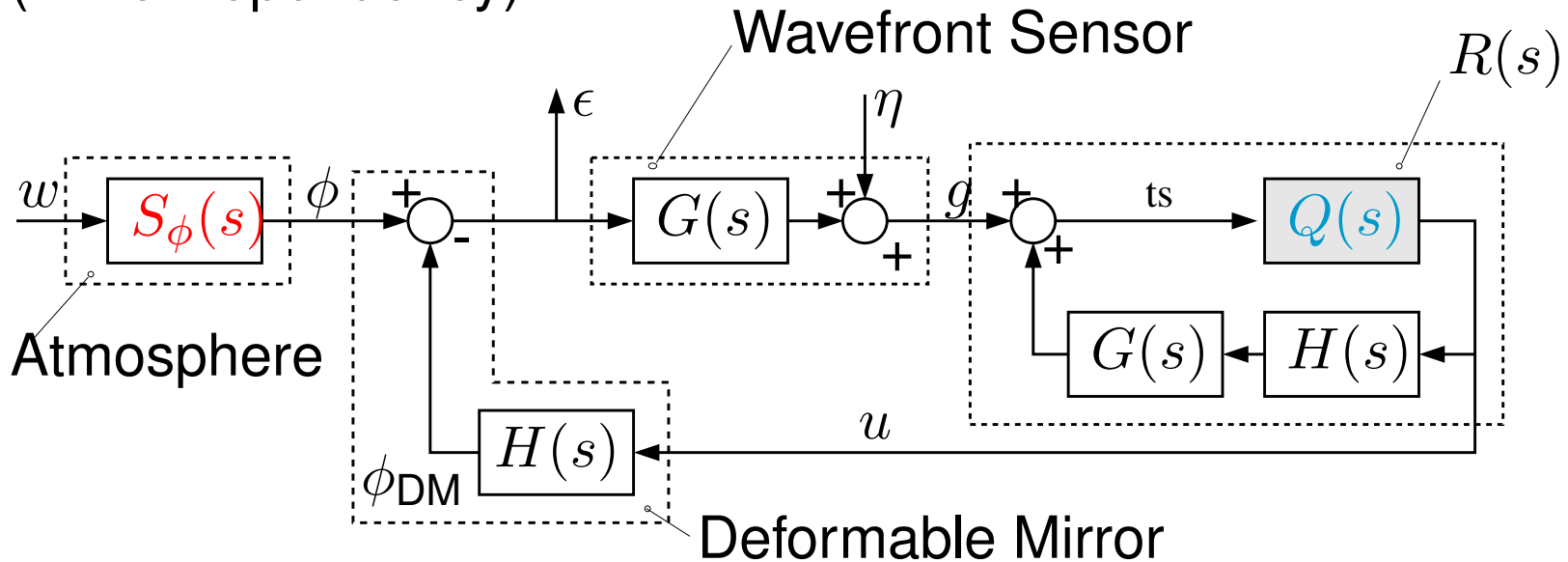


# Comparison Standard AO solution with IMC



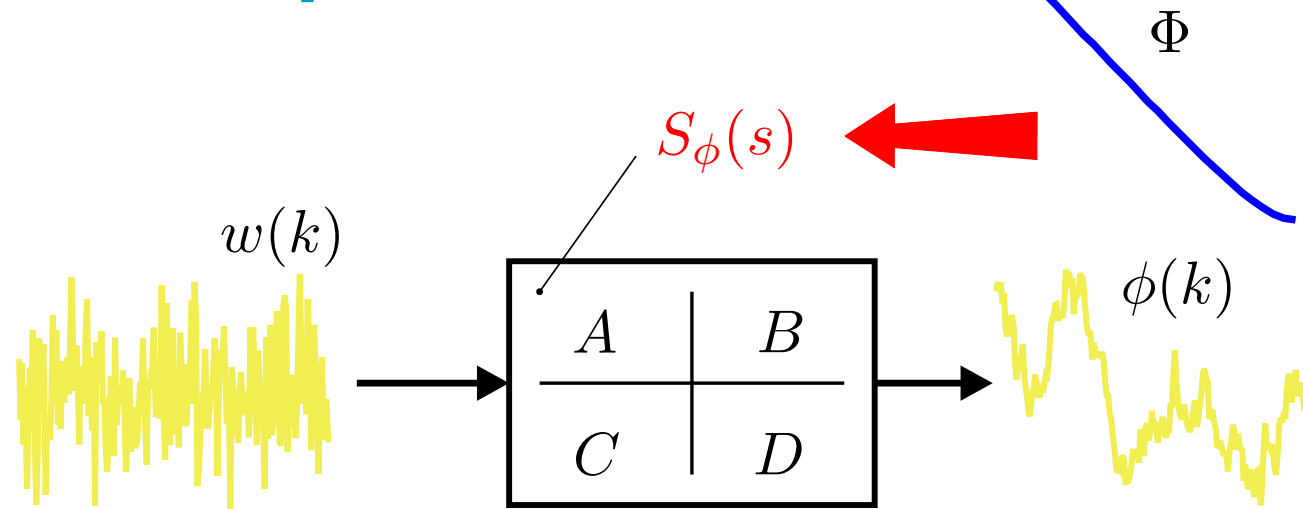
# Control Engineering Approach to AO

(Time Dependency)



$$\min_{Q(s)} \|\epsilon\|_2^2 = \min_{Q(s)} \left\| \left( I - H(s)Q(s)G(s) \right) S_\phi(s) \right\|_2 \rightarrow \begin{cases} \text{SENSITIVITY MIN.} \\ \text{SPECTRAL FACT..} \end{cases}$$

# Data Driven Spectral Factorization Problem



Given  $N + 1$  equidistantly distributed samples of a physical meaningful *matrix valued* power-spectrum:

$$\Phi_k = \Phi_y(e^{j(2\pi k/2N)}), \quad k = 0, \dots, N, \quad \Phi_k \in \mathbb{C}^{l \times l},$$

estimate the state-space quadruple  $[A, B, C, D]$  of the spectral factor  $S_\phi(z)$  as accurately as possible . . .

# Performance criterion

More specifically, determine the spectral factor

$$S_\phi : \begin{cases} x_{k+1} = Ax_k + Bw_k \\ \phi_k = Cx_k + Dw_k \end{cases}$$

such that:

- $S_\phi(z)$  is *stable*, i.e.  $|\lambda_i(A)| < 1, \forall i \in \{1, \dots, n\}$
- $S_\phi(z)$  is *minimum phase*, i.e.  $|\lambda_i(A - BD^{-1}C)| < 1$
- and the following *cost-function* is minimized:

$$J(A, B, C, D) = \sum_{k=0}^N \left\| \left( \Phi_k - S_\phi(z_k) S_\phi^T(1/z_k) \right) \circ W_k \right\|_F^2,$$

with  $W_k$  a weighting function and  $z_k := e^{j(2\pi k/2N)}$ .

# Conic linear program

$$\min_{\gamma} \text{ s.t. } \left\| \text{vec} \left\{ \left( \Phi_k - L_{AC}(z_k) Q_{BD} L_{AC}(1/z_k) \right) \circ W_k \right\}_k \right\|_2 \leq \gamma, \quad Q_{BD} \succcurlyeq 0$$
$$\min_z \{ b^T z \mid c - E^T z \succcurlyeq_{\mathcal{K}} 0 \}, \quad \mathcal{K} := \mathcal{K}_l \times \mathcal{K}_s$$

with

$$z := \begin{bmatrix} \gamma \\ \text{vec}(Q_{BD}) \end{bmatrix}, \quad b^T := \left[ 1 \mid 0_{1 \times (n+l)^2} \right] \Rightarrow b^T z = \gamma$$

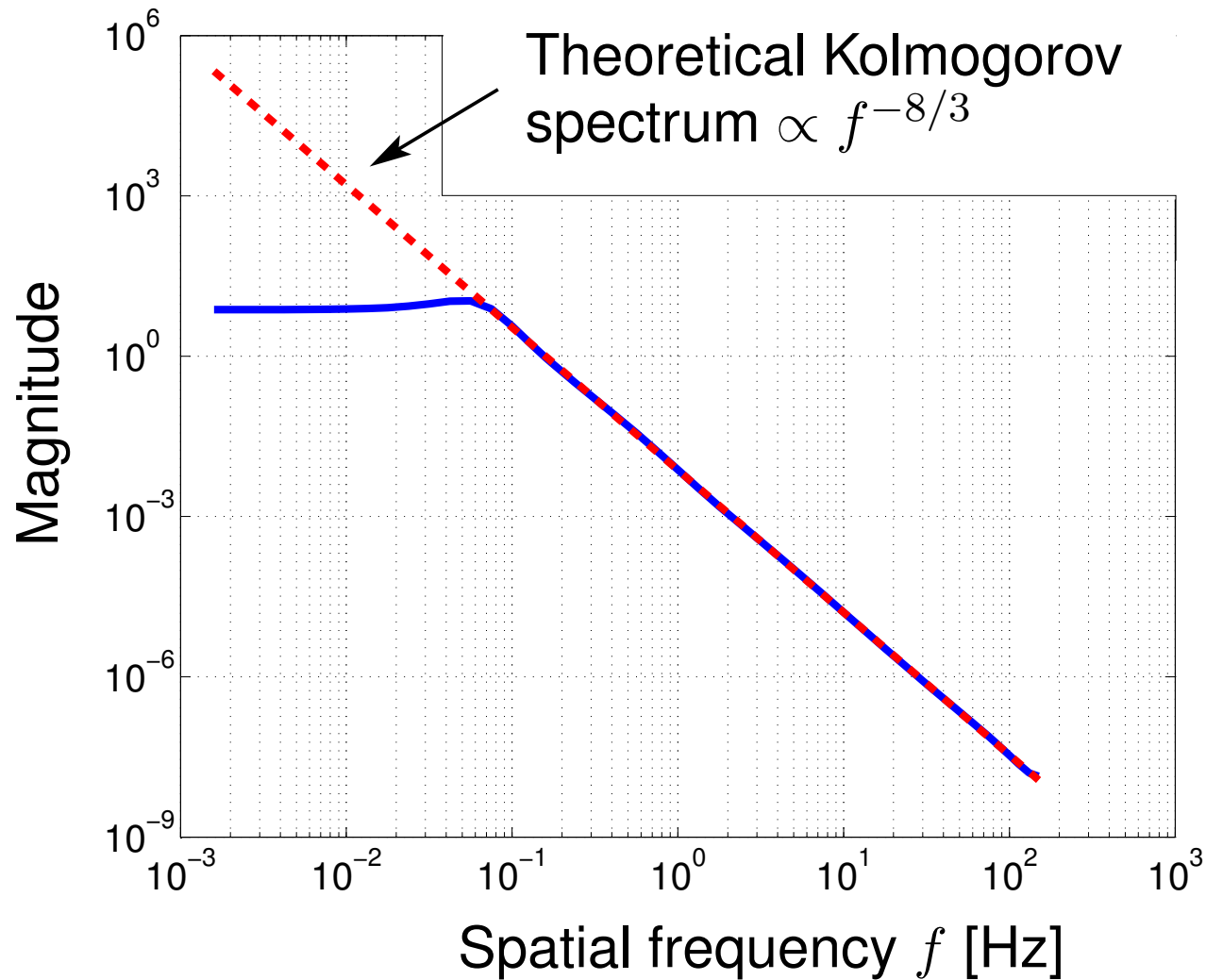
and  $c$  and  $E^T$  such that:

$$c - E^T z = \begin{bmatrix} \gamma \\ \square \\ \text{vec}(Q_{BD}) \end{bmatrix}$$

The conic linear program is efficiently solved by the Matlab toolbox **SEDUMI**, developed by J. Sturm.



# Kolmogorov power spectrum approximation

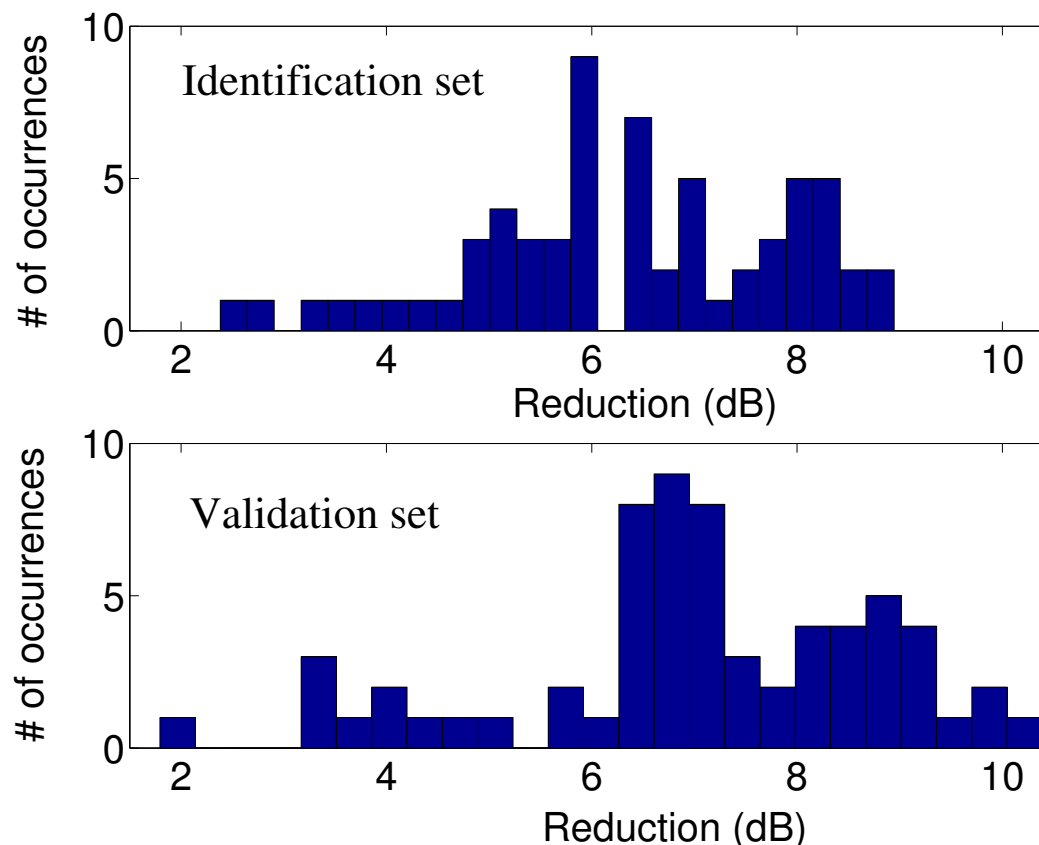


# Performance SSAR(X) algorithm

Using real-life data from William Herschel Telescope (La Palma, Canary Islands), 1997 with an  $8 \times 8$  Shack-Hartmann WFS.

( $\ell = 64, s = 50, n = 41$ )

Reduction prediction error w.r.t. random walk approach



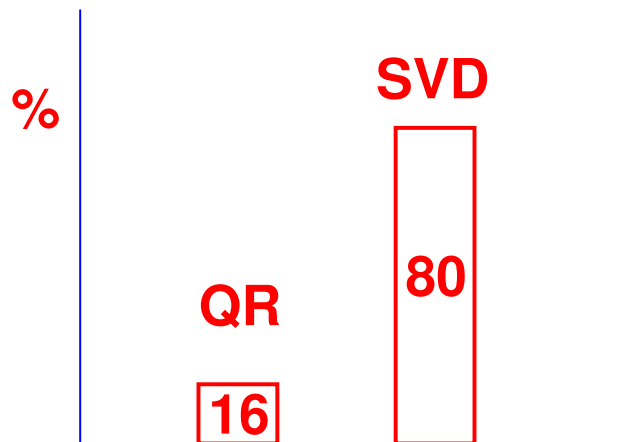
# Efficiency SSAR(X) algorithm

Main Algorithmic Steps in Calculating  $(A, C) \in (\mathbb{R}^n, \mathbb{R}^\ell)$

- QR factorization of Block-Hankel matrices  $\in \mathbb{R}^{2s\ell \times N}$
- SVD of lower triangular matrix

# Efficiency SSAR(X) algorithm

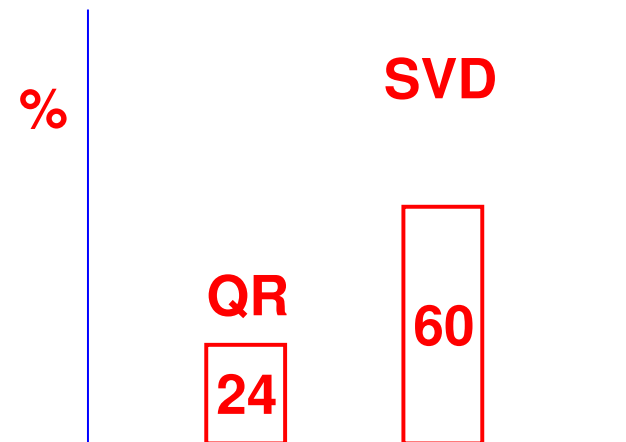
**"Standard" Matlab**  
**3392 sec**



**Slicot**

- Hankel structure
- lower triangular form

**1529 sec**



# Concluding Remarks

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