Online Nonlinear Identification of the Effect of Drugs in Anaesthesia Using a Minimal Parameterization and BIS Measurements

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Abstract—This paper addresses the problem of modeling and identification of the Depth of Anaesthesia (DoA). It presents a new MISO Wiener model for the pharmacokinetics and pharmacodynamics of propofol and remifentanil, when jointly administered to patients undergoing surgery. The models most commonly used to describe the effect of drugs in the human body are overparameterized Wiener models. In particular, in an anaesthesia environment, the high number of patient-dependent parameters coupled with the insufficient excitatory pattern of the input signals (drug dose profiles) and the presence of noise make robust identification strategies difficult to find. In fact, in such clinical application the user cannot freely choose the input signals to enable accurate parameter identification. A new MISO Wiener model with only four parameters is hence proposed to model the effect of the joint administration of the hypnotic propofol and the analgesic remifentanil. An Extended Kalman Filter (EKF) algorithm was used to perform the nonlinear online identification of the system parameters. The results show that both the new model and the identification strategy outperform the currently used tools to infer individual patient response. The proposed DoA identification scheme was evaluated in a real patient database, where the DoA is quantified by the Bispectral Index Scale (BIS) measurements. The results obtained so far indicate that the developed approach will be a powerful tool for modeling and identification of anaesthetic drug dynamics during surgical procedures.

1. INTRODUCTION

The starting point for the mathematical modeling of physiological systems is usually the background knowledge of the chemical or physical laws present in such systems. In this sense, the deduced model variables are meaningful and can easily be interpreted as masses, volumes or even temperatures. The human response to the administration of drugs in anaesthesia is a good example of this. In what concerns depth of anaesthesia (DoA), the response for the administration of hypnotics and analgesics is commonly modeled as an high order pharmacokinetic/pharmacodynamic (PK/PD) Wiener model [1]. Here the parameters to be identified are compartment volumes, micro-constant rates for mass transfers between compartments and drug clearances in the human body.

System identification theory states that the identified model is a compromise between the richness of the data and the identifiability of the parameters [2]. The application of system identification strategies to identify each patient response to drug administration in anaesthesia is a particularly complex issue. This is because a common feature of such systems is the poor excitation, meaning that the input signals (administered drug doses) are not rich enough in frequency and amplitude to excite all modes of the system [3], as it is usually modeled. This is so since the data is obtained from the surgery room, where patient safety is the prime concern. The tradeoff between complexity and identifiability is therefore addressed with minimal modeling in the present paper.

The effect of drugs in the human body can often be modeled by a linear mixing dynamics, in cascade with a static nonlinear function that describes the effect of the drug. As a consequence of this Wiener structure (a linear block in series with a static nonlinearity [4]), the prediction of human response to drugs cannot be accurately performed by linear models [5], [6]. Moreover, and in order to address the problem of having to deal with a model with many parameters, [7] presents a simplification of the model structure. In [7] it is also pointed out that to obtain a good modeling of the response, a good estimation of the PK model is needed. This fact gives rise to the problem of selecting the best structure to model the real cases. This idea was further developed in [8], where excellent results were obtained by nonlinear recursive identification of the neuromuscular blockade level using a two parameter model.

The contribution of this paper is to present a new method for nonlinear identification of the effect of drugs in anaesthesia, by the use of a new minimally parameterized Multiple-Input-Single-Output (MISO) Wiener model. As expected, this approach leads to a model whose parameters have a reduced physiological meaning. However, even from the clinical point of view, this is not a crucial issue since improved results are achieved in what concerns parameter adaptation and output signal tracking. Furthermore, continuous time parameters are estimated, a fact that facilitates physiological interpretation.

The input signals consist of the dosage of propofol and remifentanil. The human effect output signal used in the paper is the clinically-validated electroencephalogram-derived Bispectral Index Scale (BIS) [9]. It can be noted that the BIS is at the focal point of anaesthesia research today. Ranging from 100% (completely “awake” clinical state) to 0% (isoelectric EEG) the BIS is widely used as an indicator of the DoA. In a general surgery environment, the BIS
should be kept between 40% and 60% to enable a faster emergence from anaesthesia [10] and a lower administered drug dosage [11]. The combined administration of hypnotics and analgesics for induction and maintenance of DoA is a common practice. The hypnotic is targeted to the loss of consciousness and prevents awareness, while the analgesic is given to suppress pain. Indeed, the clinical advantage of this combined procedure is the synergistic increase in the expected effects of both drugs based on the nonlinear concentration–effect relationships of the individual agents [12]. This evidence is modeled by a nonlinear interaction function between the two drugs.

The present paper is structured as follows. Section II describes the state of the art of DoA modeling, while Section III presents both the linear and nonlinear parts of the new minimally parameterized model for the BIS response. In Section IV the algorithm is derived, followed by the presentation of results when applied to patient data in Section V. Conclusions follow in Section VI.

II. DoA: STATE OF THE ART MODELS

The most commonly used models in the literature to describe the PK and PD of the propofol (hypnotic) and remifentanil (analgesic) effects in the human body are described in this section. It should be stressed that these models will not be the ones used for the development of the identification methodologies of this study. These models are discussed here to point out the need for the development of new minimally parameterized models to match the parsimony principle of system identification [2].

A. Linear part

The PK models describe mixing dynamics of the drugs in the different theoretical compartments of the human body [13]. Both for propofol and remifentanil, a 3-compartment mammillary model is normally used [14], [15]. As illustrated in Fig. 1, the drug (considered as the system input) is intravenously administrated, entering in the main compartment with infusion rate \( r(t) \) [mg ml\(^{-1}\) min\(^{-1}\)]. The clearance of the drug, modeled by an outer flow of the main compartment \( k_{10} \) [min\(^{-1}\)], and the transfer coefficients \( k_{ij} \) [min\(^{-1}\)] from compartment \( i \) to \( j \) are patient dependent parameters.

By direct deduction from mass balances between compartments, and assuming that for each compartment \( i \), a concentration \( x_i(t) \) [mg ml\(^{-1}\)] of drug is present, the state space representation that is commonly used becomes

\[
\dot{x}(t) = \begin{pmatrix}
\dot{x}_1(t) \\
\dot{x}_2(t) \\
\dot{x}_3(t)
\end{pmatrix} = \begin{pmatrix}
-(k_{10} + k_{12} + k_{13}) & \frac{k_{21} V_2}{V_1} & \frac{k_{31} V_3}{V_1} \\
\frac{k_{12} V_2}{V_1} & -k_{21} & 0 \\
\frac{k_{13} V_3}{V_1} & 0 & -k_{31}
\end{pmatrix} x(t) + \begin{pmatrix}
1 \\
0 \\
0
\end{pmatrix} r(t),
\]

where \( V_i \) [ml] represents the volume of compartment \( i \).

The PD nonlinearity relates the drug concentration with the effect, DoA, and has a first linear dynamic part approximated by a first order differential equation [16]

\[
\dot{y}(t) = k_{e0}(x_1(t) - x_e(t)),
\]

where \( k_{e0} \) is the inverse of the equilibrium time between the central compartment (compartment 1 in Fig. 1) and the effect compartment, and \( x_e(t) \) [mg ml\(^{-1}\)] is the effect compartment concentration (which cannot be measured).

In clinical practice, population models are applied to infer the response of each patient to a certain drug administration profile. For propofol, the parameters from Marsh [17] or from Schnider [18] are usually used, whereas for remifentanil, the parameters from Minto [15] are commonly applied.

B. Nonlinear interaction

This section describes the widely accepted nonlinear model for the interaction between propofol and remifentanil [19]. It relates the effect concentration of both drugs with the electroencephalographic parameter values e.g. BIS. Both effect concentrations \( x_{e,prop}(t) \) and \( x_{e,remi}(t) \) are first normalized with respect to their concentration at half the maximal effect (\( EC_{50}^{prop} \) and \( EC_{50}^{remi} \), respectively), i.e.

\[
U_{prop}(t) = \frac{x_{e,prop}(t)}{EC_{50}^{prop}}, \quad U_{remi}(t) = \frac{x_{e,remi}(t)}{EC_{50}^{remi}}.
\]

As mentioned before, since the interaction of propofol and remifentanil is not purely additive, the potency of the drug mixture is modeled as follows

\[
\phi = \frac{U_{prop}(t)}{U_{prop}(t) + U_{remi}(t)},
\]

where, by definition, \( \phi \) ranges from 0 (remifentanil only) and 1 (propofol only). The nonlinear concentration–response relationship for any ratio of the two drugs can then be described by a generalized Hill equation as

\[
y(t) = y_0 \left(1 - \frac{\left(U_{prop}(t)+U_{remi}(t)\right)^\gamma}{\left(U_{prop}(t)+U_{remi}(t)\right)^\gamma + \phi}\right),
\]
where \( y_0 \) is the effect at zero concentration, \( \gamma \) controls the steepness of the nonlinear concentration-response relation, and \( U_{50}(\phi) \) is the number of units associated with 50\% of the maximum effect of both drugs at ratio \( \phi \). In [19] a quadratic polynomial was proposed for the expression of \( U_{50}(\phi) \):

\[
U_{50}(\phi) = 1 - \beta \phi + \beta \phi^2 .
\]

In common clinical practice, the parameters \( \gamma, \beta, EC_{50}^{\text{prop}} \) and \( EC_{50}^{\text{remi}} \) and the linear parameters \( k_i \) and \( k_e \) from (1) and (2) are usually guessed based on population model distributions and on the clinicians’ expertise. The result is a model depending on many continuous time parameters.

III. MINIMALLY PARAMETERIZED MODEL

A new MISO Wiener model with a minimal number of parameters describing the joint effect of propofol and remifentanil in the human body is presented in this section. Models are first built using a continuous-time description and then sampled with a zero-order hold strategy. This makes it possible to derive algorithms that estimate the underlying continuous time parameters, exploiting the intrinsic feature of having a minimal number of parameters.

A. Linear block

By inspection of the model structure, the plasmatic concentration (in compartment 1 of Fig. 1) and the effect concentration coming from population studies for both propofol [18] and remifentanil [15], a third-order continuous time model is proposed for the linear dynamics of each drug. It can be noted that this approach was also very successful in [8].

Propofol linear dynamics is hence modeled by

\[
\dot{X}_e^{\text{prop}}(s, \alpha) = \frac{k_1 k_2 k_3 \alpha^3}{(s + k_1 \alpha)(s + k_2 \alpha)(s + k_3 \alpha)} R^{\text{prop}}(s),
\]

where \( X_e^{\text{prop}}(s, \alpha) \) is the Laplace transform of the output from the model linear dynamic part for propofol \( \dot{x}_{\text{prop}}(t, \alpha) \) and \( R^{\text{prop}}(s) \) is the Laplace transform of the input signal \( r^{\text{prop}}(t) \). The pole location \( \alpha \) is selected as the parameter to be identified.

Remifentanil linear dynamics is similarly modeled by

\[
\dot{X}_e^{\text{remi}}(s, \eta) = \frac{l_1 l_2 l_3 \eta^3}{(s + l_1 \eta)(s + l_2 \eta)(s + l_3 \eta)} R^{\text{remi}}(s),
\]

where \( X_e^{\text{remi}}(s, \eta) \) is the Laplace transform of the output from the model for remifentanil \( \dot{x}_{\text{remi}}(t, \eta) \) and \( R^{\text{remi}}(s) \) is the Laplace transform of the input signal \( r^{\text{remi}}(t) \). The pole location \( \eta \) is selected as the parameter to be identified.

B. Nonlinear block

Using the model in (5) as starting point, a new formulation for the nonlinearity is now proposed. According to (6),

\[
\frac{\dot{U}_{\text{prop}}(t, \alpha) + \dot{U}_{\text{remi}}(t, \eta)}{U_{50}(\phi)} = \frac{\dot{U}_{\text{prop}}(t, \alpha) + \dot{U}_{\text{remi}}(t, \eta)}{1 - \beta \phi + \beta \phi^2}.
\]

Hence, to motivate the new model, consider \( |r| = \beta \phi - \beta \phi^2 \) to be less than 1 and exploit the Taylor series expansion

\[
\frac{1}{1 - r} = 1 + r + r^2 + r^3 + \ldots
\]

Then, neglecting the high-order terms, and substituting \( \phi \) according to (4), it follows

\[
\frac{\dot{U}_{\text{prop}}(t, \alpha) + \dot{U}_{\text{remi}}(t, \eta)}{U_{50}(\phi)} = \left( \dot{U}_{\text{prop}}(t, \alpha) + \dot{U}_{\text{remi}}(t, \eta) \right) \left( 1 + \beta \frac{\dot{U}_{\text{prop}}(t, \alpha)}{U_{50}(\phi)} \right) = \dot{U}_{\text{remi}}(t, \eta) + (1 + \beta) \dot{U}_{\text{prop}}(t, \alpha) = \dot{U}_{\text{remi}}(t, \eta) + m \dot{U}_{\text{prop}}(t, \alpha).
\]

Here \( m = 1 + \beta \) is selected as one of the parameters to be identified. Furthermore, following (3),

\[
\dot{U}_{\text{prop}}(t, \alpha) = \frac{x^{\text{prop}}(t, \alpha)}{EC_{50}^{\text{prop}}}, \quad \dot{U}_{\text{remi}}(t, \eta) = \frac{x^{\text{remi}}(t, \eta)}{EC_{50}^{\text{remi}}}.
\]

Hence, (5) is substituted by the new formulation:

\[
\hat{y}(t) = \frac{y_0}{1 + \left( U_{\text{remi}}(t, \eta) + m U_{\text{prop}}(t, \alpha) \right) ^\gamma}.
\]

C. Total model

For the new proposed model several quantities are fixed or determined offline. Similarly as in [8], the parameters \( k_i \) and \( l_i, i = 1, \ldots, 3 \) are determined by the use of batch identification over a large database of patient data. The batch identification is beyond the scope of this paper, see [20] for details. Note that \( k_1 = l_1 = 1 \) needs to hold to get a unique parameterization. The normalizing constants \( EC_{50}^{\text{prop}} \) and \( EC_{50}^{\text{remi}} \) are also fixed (similarly to the work in [21]). When using BIS as the parameter to infer the DoA, \( y_0 \) in the nonlinear block is equal to 97.7 due to monitor restrictions.

The linear part of the system is then parameterized in the frequency domain as (7) and (8) with the systems inputs being the propofol rate \( r_{\text{prop}}(t) \) and remifentanil rate \( r_{\text{remi}}(t) \), respectively. After normalizing the outputs of the linear part \( \dot{x}_e^{\text{prop}}(t, \alpha) \) and \( \dot{x}_e^{\text{remi}}(t, \eta) \) with respect to \( EC_{50}^{\text{prop}} \) and \( EC_{50}^{\text{remi}} \) (according to (12)), the model output \( \hat{y}(t) \) is obtained through the nonlinear function (13). The total parameter vector to be identified is then

\[
\theta = (\alpha \quad \eta \quad m \quad \gamma)^T.
\]

IV. RECURSIVE IDENTIFICATION ALGORITHM: EXTENDED KALMAN FILTER

A. State-space model for EKF

Aiming to implement the proposed model structure in the Extended Kalman Filter (EKF) algorithm, the discrete-time representation must be written in state-space form. As an intermediate step, the representations (7) and (8) are transformed into a joint continuous time state-space form (16) describing the linear dynamics of each drug.
Due to the fact that the synergistic interaction between propofol and remifentanil of (12) is no more nonlinear, the linear state-space output $\ddot{z}(t)$ will be the result from the linear weighted sum in (12)

$$\ddot{z}(t) = \dot{U}_{\text{remi}}(t, \eta) + m \dot{U}_{\text{prop}}(t, \alpha).$$

(15)

Hence, the continuous-time representation becomes

$$\dot{\hat{z}}(t) = A(\alpha, \eta) \hat{x}(t) + B r(t),$$

$$\ddot{\hat{z}}(t) = C(\theta) \dot{\hat{x}}(t),$$

with

$$A(\alpha, \eta) = \left( \begin{array}{c} A_p(\alpha) \\ 0_{(3x3)} \\ A_r(\eta) \end{array} \right),$$

(17)

where $A_p(\alpha) \in \mathbb{R}^{3 \times 3}$ is the system matrix for propofol (deduced from (7)) and $A_r(\eta) \in \mathbb{R}^{3 \times 3}$ is the system matrix for remifentanil (deduced from (8)). In (16), $B$, $r(t)$ and $C(\theta)$ are as following

$$B = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{pmatrix}^T,$$

(18)

$$r(t) = \begin{pmatrix} r_{\text{prop}}(t) \\ r_{\text{remi}}(t) \end{pmatrix}^T,$$

(19)

$$C(\theta) = \begin{pmatrix} 0 & 0 & \frac{k_1 \alpha k_3 \eta^3}{EC_{50}} \\ 0 & 0 & \frac{k_2 \alpha \eta^3}{EC_{50}} \end{pmatrix}.$$

(20)

Finally, the nonlinear output is obtained from (13) as

$$\hat{y}(t) = \frac{y_0}{1 + (\ddot{\hat{z}}(t))} = \frac{y_0}{1 + (\ddot{\hat{z}}(t))}.$$

(21)

The main reason for the use of the EKF is the possibility to obtain the parameter estimates along with system state estimates online. In comparison with other recursive identification techniques, it enables the independent tuning using the covariance matrix of both the process and measurement noise, thereby giving rise to an independent tuning of the convergence speed for each parameter. To describe the EKF the general discrete time nonlinear model

$$\begin{align*}
\hat{x}(k+1) &= f(k, \hat{x}(k), r(k)) + g(k, \hat{x}(k)) v(k) \\
\hat{y}(k) &= h(k, \hat{x}(k)) + e(k),
\end{align*}$$

(22)

is used, where $v(k)$ and $e(k)$ are mutually independent Gaussian white noise sequences with zero mean and covariances given by $R_1(k)$ and $R_2(k)$, respectively. The EKF algorithm can then be summarized as follows [22]:

$$H(k) = \frac{\partial h(k, x)}{\partial x} \bigg|_{x = \hat{x}(k|k-1)},$$

$$K(k) = P(k|k-1) H^T(k) \times [H(k) P(k|k-1) H^T(k) + R(k)]^{-1},$$

$$\hat{x}(k|k) = \hat{x}(k|k-1) + K(k) [y(k) - h(k, \hat{x}(k|k-1))],$$

$$P(k|k) = P(k|k-1) - K(k) H(k) P(k|k-1) H^T(k),$$

$$\dot{\hat{x}}(k+1|k) = f(k, \hat{x}(k|k), r(k)),$$

$$F(k) = \frac{\partial f(k, x)}{\partial x} \bigg|_{x = \hat{x}(k|k)},$$

$$G(k) = g(k, x) \bigg|_{x = \hat{x}(k|k)},$$

$$P(k+1|k) = F(k) P(k|k) F^T(k) + G(k) R_1(k) G^T(k).$$

(23)

$$\dddot{\hat{z}}(kh + h) = \Phi(\alpha, \eta) \dddot{\hat{z}}(kh) + \Gamma(\alpha, \eta) r(kh)$$

$$\dddot{\hat{z}}(kh) = C(\theta) \dddot{\hat{x}}(kh)$$

$$\dddot{\hat{y}}(kh) = \frac{y_0}{1 + (\dddot{\hat{z}}(kh))}.$$ 

(24)

$$\Phi(\alpha, \eta) = e^{A(\alpha, \eta) h},$$

$$\Gamma(\alpha, \eta) = \int_0^h e^{A(\alpha, \eta)s} ds B.$$ 

(25)

Here, $r(kh) \in \mathbb{R}^{2 \times 1}$ is the input (piecewise constant drug dose infusion for both propofol and remifentanil, according to (19)), $\hat{x}(kh) \in \mathbb{R}^{6 \times 1}$ the discrete model state-vector, $\dddot{\hat{z}}(kh) \in \mathbb{R}$ is the linear output (joint effect resulting from the interaction between the two drugs), $\Phi(\alpha, \eta) \in \mathbb{R}^{6 \times 6}$ and $\Gamma \in \mathbb{R}^{6 \times 1}$, being the sampled system matrices. The model output is given by $\dddot{\hat{y}}(kh)$.

A common strategy to enable the estimation of model parameters with the EKF is the introduction of an augmented state [2]. Hence, the model for the EKF estimation brings together the sampled model (24) and a random walk model for the parameter estimates [2]. Using (14), the augmented state vector becomes

$$\dddot{\hat{x}}(kh) = \begin{pmatrix} \dddot{\hat{x}}_1(kh + h) \\ \vdots \\ \dddot{\hat{x}}_6(kh + h) \end{pmatrix} = \begin{pmatrix} \dddot{\hat{x}}_1(kh + h) \\ \vdots \\ \dddot{\hat{x}}_{10}(kh + h) \end{pmatrix}.$$ 

(26)

Hence, the augmented state-space model becomes

$$\dddot{\hat{z}}(kh + h) = \Phi(\alpha, \eta) \begin{pmatrix} 0_{(6 \times 4)} \\ I \end{pmatrix} \dddot{\hat{z}}(kh)$$

$$+ \Gamma(\alpha, \eta) r(kh) + w(kh)$$

$$= \begin{pmatrix} f_1(kh, \dddot{\hat{x}}(kh), r(kh)) \\ \vdots \\ f_{10}(kh, \dddot{\hat{x}}(kh), r(kh)) \end{pmatrix} + w(kh).$$ 

(27)
\[ \hat{y}(kh) = \frac{y_0}{1 + (C(\theta)\hat{x}(kh))^T\hat{x}_{10}(kh)} \equiv h(kh, \hat{x}(kh)) + e(kh), \quad (28) \]
\[ C(\theta) = \begin{pmatrix} C(\theta) & 0 & 0 & 0 & 0 \end{pmatrix}. \quad (29) \]

C. Linearization and Initialization

In the EKF algorithm structure (23), it is necessary to linearize both \( f(k, x) \) and \( h(k, x) \). Both linearizations were performed analytically. The formulas for \( F(kh) \) and \( H(kh) \) are not shown here due to their complexity.

After having formulated all the quantities needed to set up the EKF, the initial values for the variables must be specified. The initial values for the states were
\[ \hat{x}(0|1) = \begin{pmatrix} 0.0 & 0.0 & 0.0 & 0.0 & 0.0 \\ 0.0 & 0.2 & 0.2 & 0.6 & 1.0 \end{pmatrix}^T \quad (30) \]

Using simulations performed on the available database, it was found that the diagonal matrix \( P(0|1) \) could be initialized as
\[ P(0|1) = \text{diag} \begin{pmatrix} 10^2 & 10^2 & 1^2 & 100^2 & 10^2 \\ 1 & 10 & 10 & 10 & 10 \end{pmatrix} \quad (31) \]

Performing a similar empirical analysis on the simulated signals, the values for the diagonal covariance matrix \( R_1 \) and the covariance matrix \( R_2 \) were set to
\[ R_1 = \text{diag} \begin{pmatrix} 100^2 & 100^2 & 10^2 & 1000^2 & 100^2 \\ 10^2 & 10^2 & 10^2 & 10^2 & 10^2 \end{pmatrix} \quad (32) \]
\[ R_2 = 10^{10} \quad (33) \]

V. RECURSIVE SIGNAL TRACKING RESULTS

This section presents examples of the EKF performance applied to the new minimally parameterized model in Section III. Simulations were performed using the real BIS measurements from patients undergoing surgery. In these real cases in the database, the BIS signal was maintained around the level of 40. This was achieved by the action of the anesthetist who changed the infusion rates of both drugs according to the clinical goal.

The real measured BIS signal \( y(t) \) and the EKF simulated BIS signal \( \hat{y}(t) \) are illustrated in Fig. 2. The results show that the EKF simulated BIS signal tracks the real measured BIS signal excellently during the total time-window of this case study. More importantly, when the real BIS signal changes its behaviour, as at around minute 60, the estimated model signal also tracks that behaviour. Sudden changes are also tracked by the simulated signal, e.g. the rapid drop in the signal that occurs right after this increase around minute 60. Furthermore, the algorithm is able to discard the noise effects present in the measured BIS, giving rise to a filtered signal able to catch the main trends of the real signal. This capability is obtained via the parameter estimates provided by the EKF algorithm. The time evolution of the parameter estimates (\( \hat{\alpha}, \hat{\gamma}, \hat{m} \) and \( \hat{\gamma} \)) for this example are shown in Fig. 3. The input signals, propofol and remifentanil rates, that were present in this real case are the ones illustrated in Fig. 4.

It can be concluded from the plots that the new minimally parameterized Wiener model (27), (28) accurately describes the nonlinear system dynamics. By the use of the EKF strategy, model parameters can be extracted from the real BIS measurements. The tracking performance is excellent combining accurate modeling with very good noise suppression.
VI. CONCLUSIONS AND FUTURE WORK

In this work, a new minimally parameterized MISO model for the human response to anaesthesia is designed. Furthermore, an online nonlinear identification strategy of that response using real measurements is proposed. The system inputs are the propofol (hypnotic drug) and remifentanil (analgesic drug) infusion rates, and the output is the Depth of Anaesthesia (DoA) quantitative measurement Bispectral Index Scale (BIS). The new model satisfactorily describes the input-output system behaviour, having its parameters updated by the Extended Kalman Filter (EKF) identification algorithm that was derived from the new model.

The new model and algorithm address the poor excitation, the few output datapoints, and the high level of noise in the output signal. In addition to the very good BIS tracking and noise filtering achieved by the proposed identification algorithm, it can be noted that the parameter estimates are quite stationary. This is a very strong indication that the proposed minimal parameterization is in fact sufficient to describe the dynamics of the system, using a system identification perspective. This also indicates that difficulties can be expected when the standard models with many more parameters are used for identification purposes, a fact that has been reported in the literature. One other consequence of this is that the obtained parameter estimates can be expected to be very useful for controller design purposes, this being the ultimate goal for this research.

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