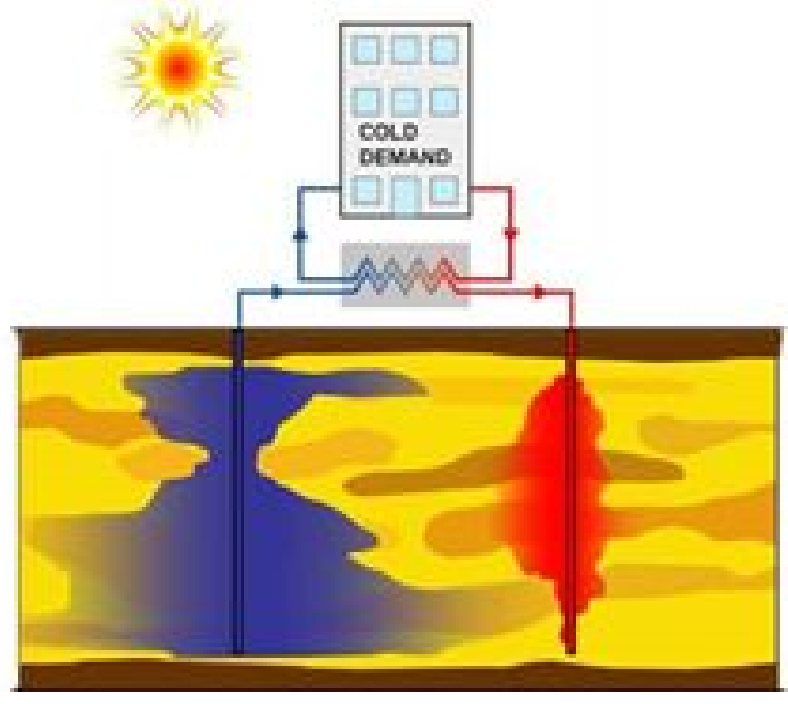


ATES System in Smart Thermal Grids

Distributed Stochastic Model Predictive Control

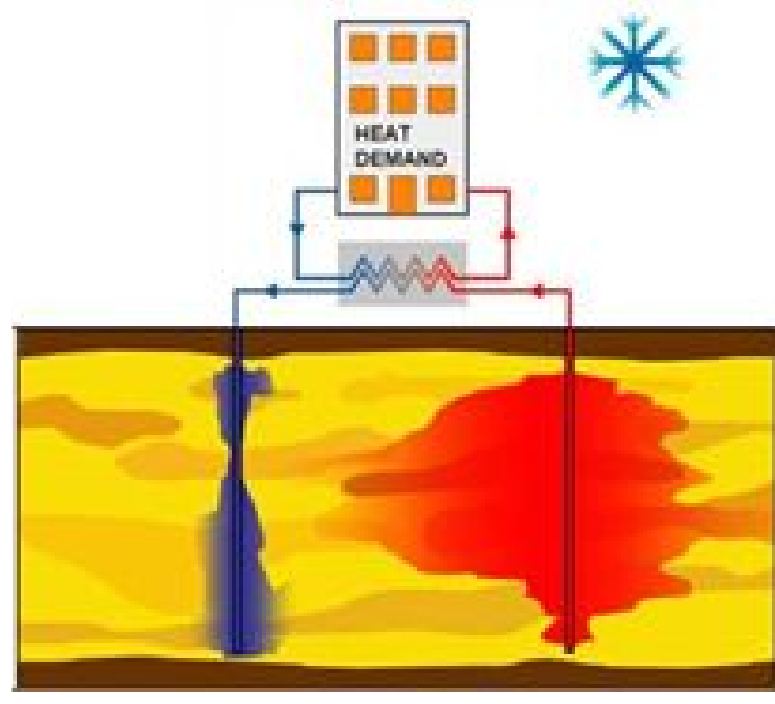
Aquifer Thermal Energy Storage (ATES)

- A large-scale natural subsurface storage for thermal energy
- An innovative method for thermal energy balance in smart grids



Warm season:

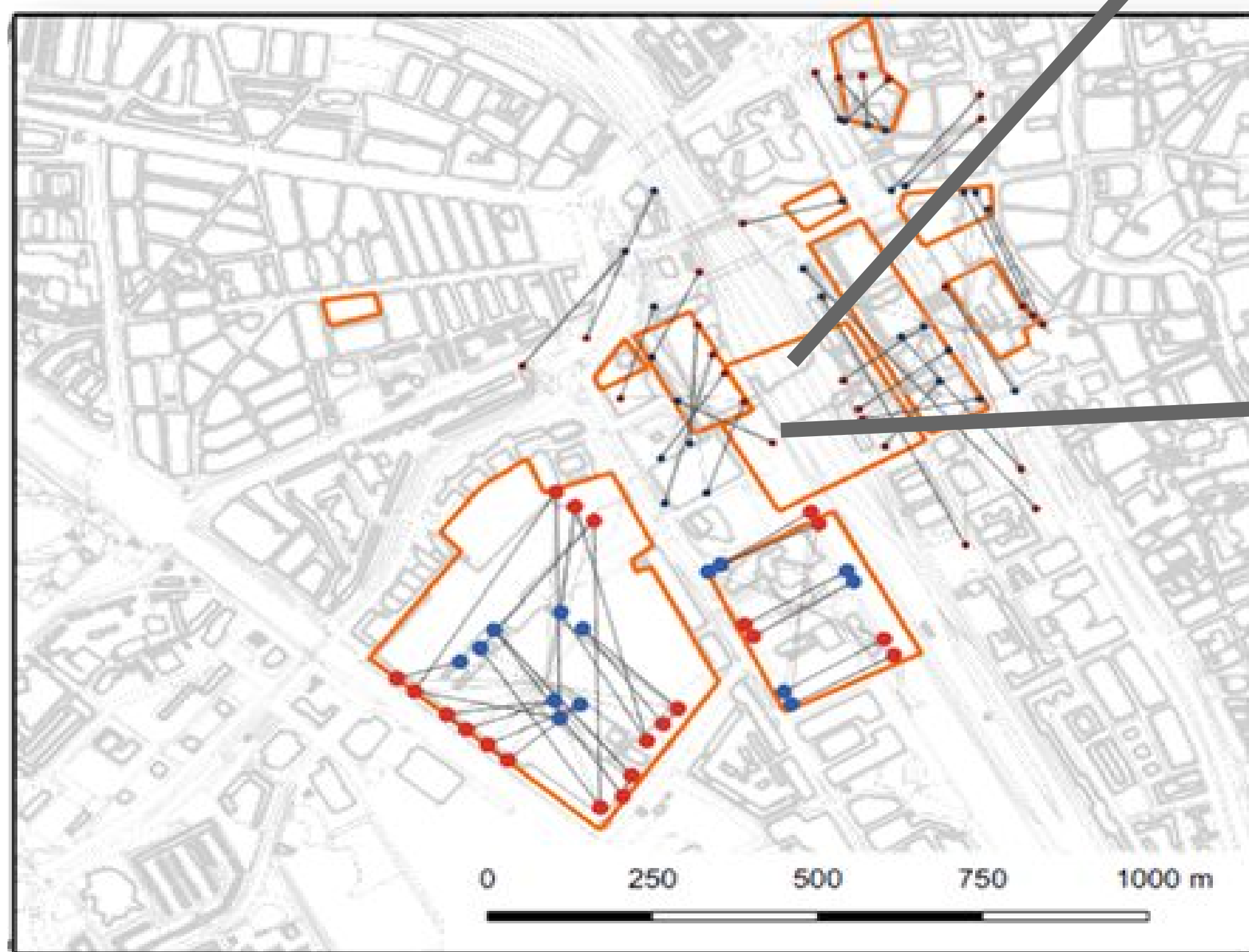
- The building requests thermal energy for the cooling purpose
- Water is injected into **warm well** and is taken from **cold well**
- The stored water contains **warm** thermal energy for next season



Cold season:

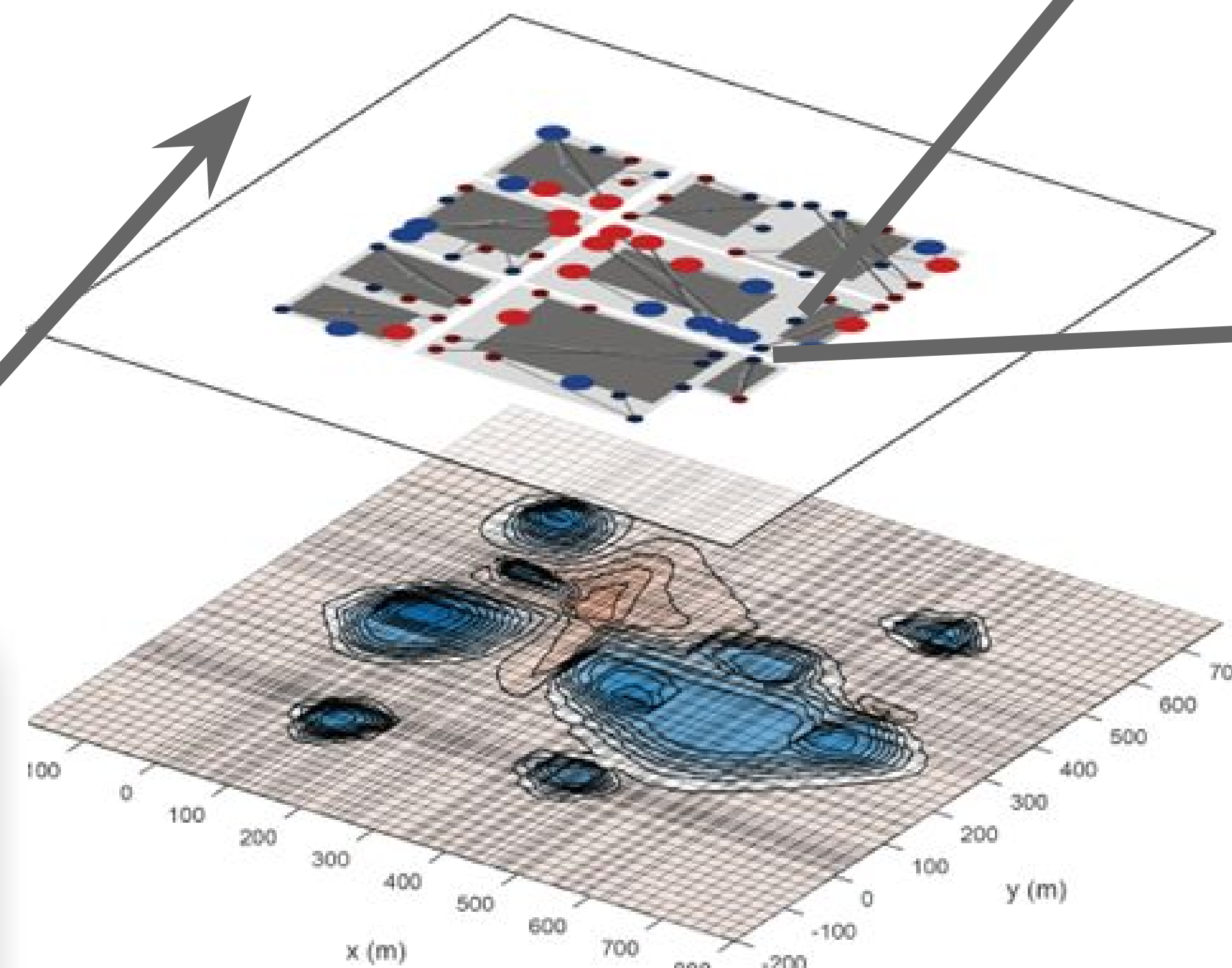
- The building requests thermal energy for the heating purpose
- Water is injected into **cold well** and is taken from **warm well**
- The stored water contains **cold** thermal energy for next season

- ATES systems act as seasonal energy storage buffers and can self-organize subsurface space use to increase efficiency

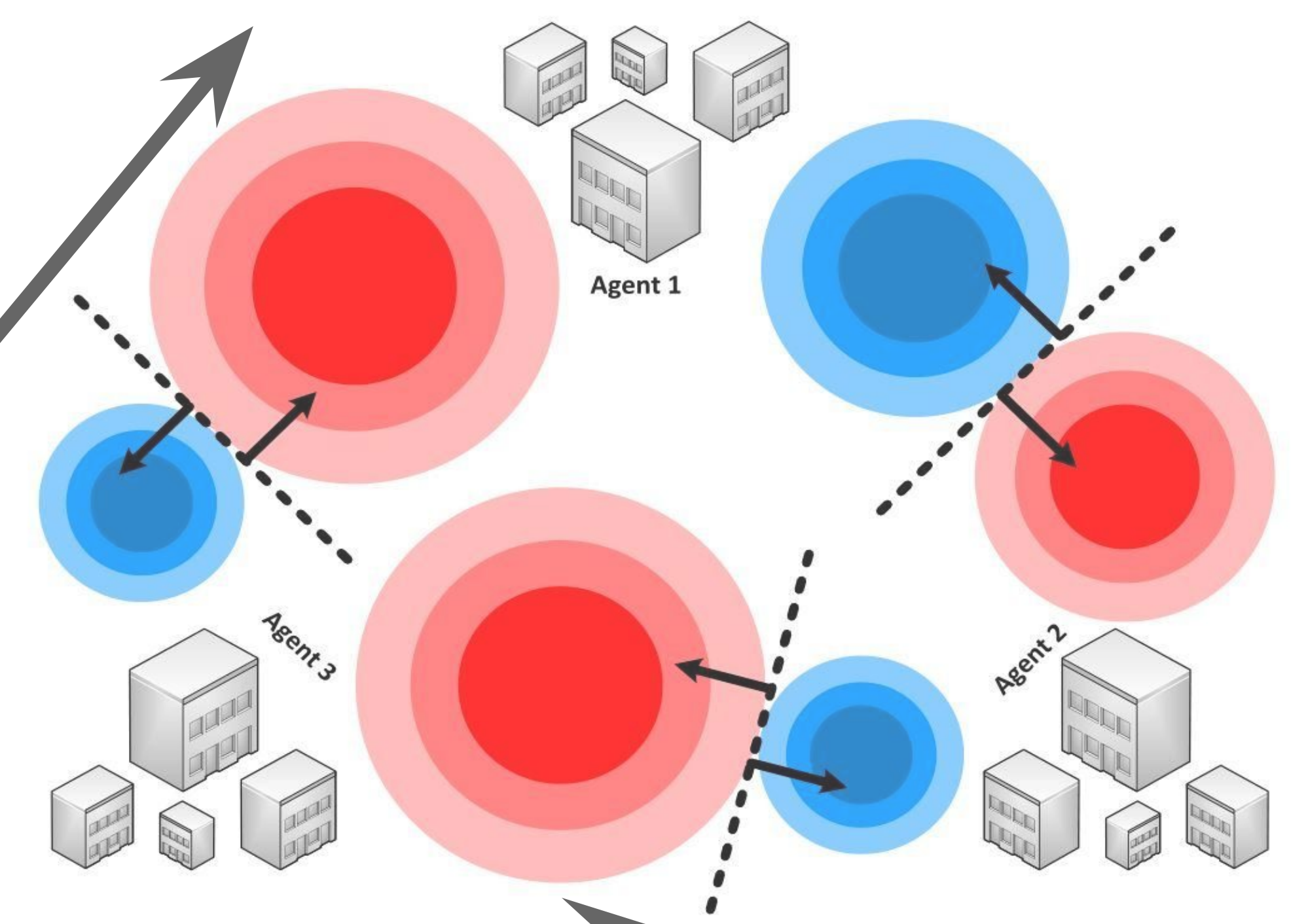


Problem Statement

- How can we develop a self-organizing system that adapts to the operational experience in a networked of interconnected ATES systems?
- How do the idealized dynamics manifest in realistic conditions under operational uncertainties?
- What kind of control framework is the best for such a network of buildings using interconnected ATES subject to the local (private) and common uncertainty sources?



ATES in Uncertain STGs



- How can we deal with such a spatially distributed system, complex multivariable, switching, nonlinear behavior when coupled with building climate controllers together with strong exogenous disturbances, stochastic uncertainty?
- The most efficient way to reduce uncertainty is to communicate (cooperate) between neighboring systems
- Investigate cooperative control schemes that allow a distributed solution of the underlying stochastic control problem

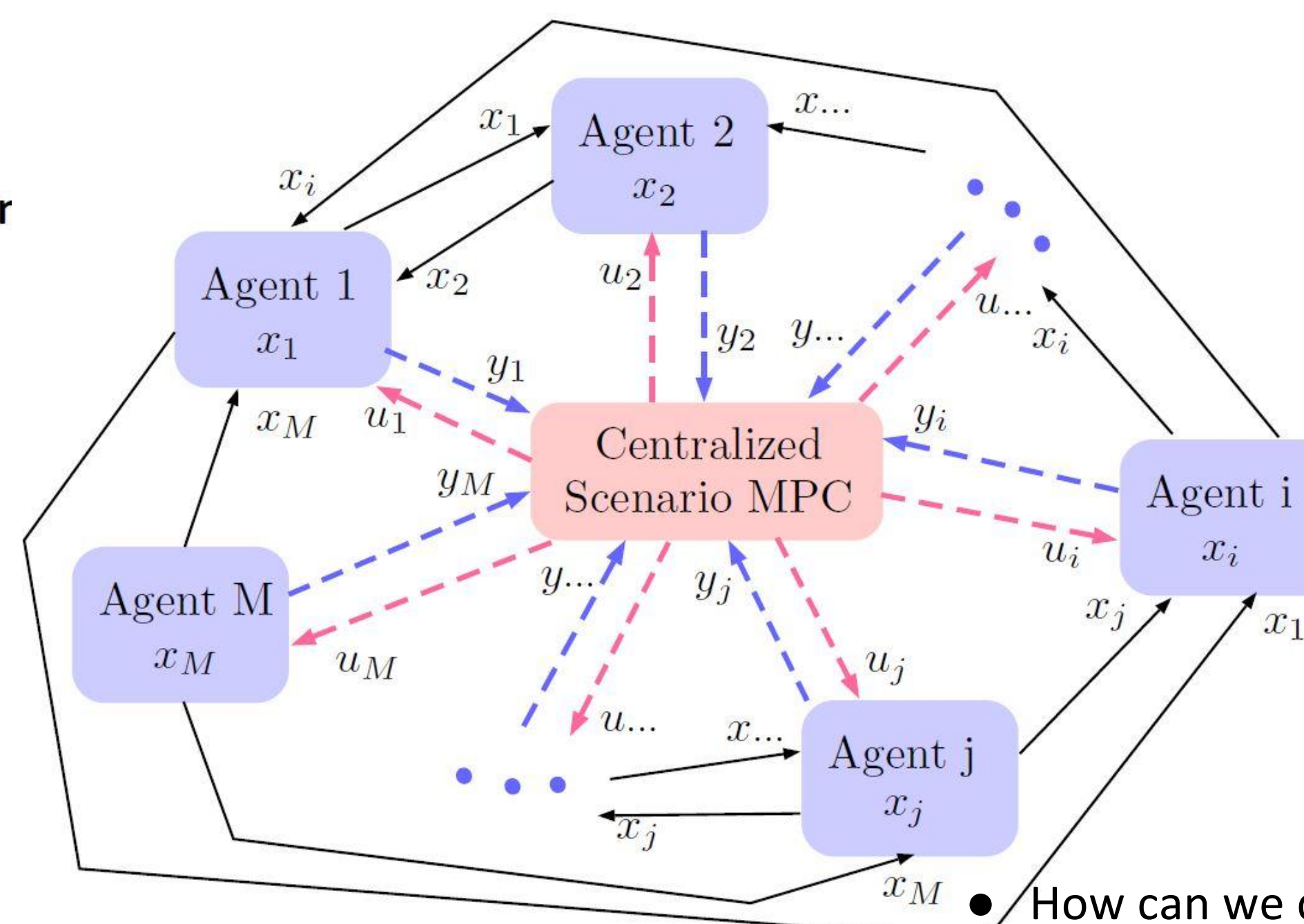
Distributed Scenario MPC (Plug-and-Play Framework)

Centralized Scenario Program

$$\begin{aligned} \min_{\{u_i\}_{i \in \mathcal{N}}} \quad & \sum_{i \in \mathcal{N}} f_i(x_{i,k}, u_{i,k}) \\ \text{s.t.} \quad & x_{i,k+1} = A_{ii}x_{i,k} + B_i u_{i,k} + C_i \delta_{i,k}^{(i)} + \sum_{j \in \mathcal{N}_i} A_{ij} x_{j,k}^{(i)}, \quad x_{i,k} = x_{i,0} \\ & x_{i,k+\ell} \in \mathcal{X}_i, \quad \forall \ell \in \mathbb{N}_+, \quad \forall \delta_{i,k}^{(i)} \in \mathcal{S}_{\delta_i} \\ & u_{i,k} \in \mathcal{U}_i, \quad \forall k \in \mathcal{T}, \quad \forall i \in \mathcal{N} \end{aligned}$$

Distributed Scenario Program

$$\begin{aligned} \min_{\{u_{i,k}\}_{i \in \mathcal{N}, k \in \mathcal{T}}} \quad & f_i(x_{i,k}, u_{i,k}) \\ \text{s.t.} \quad & x_{i,k+1} = A_{ii}x_{i,k} + B_i u_{i,k} + q_{i,k}^{(i)}, \quad x_{i,k} = x_{i,0} \\ & x_{i,k+\ell} \in \mathcal{X}_i, \quad \forall \ell \in \mathbb{N}_+, \quad \forall q_{i,k}^{(i)} \in \mathcal{S}_{q_i} \\ & u_{i,k} \in \mathcal{U}_i, \quad \forall k \in \mathcal{T} \end{aligned}$$



- How can we decompose such a dynamically coupled large-scale uncertain system?
- What are the requirements?

Probabilistic Feasibility for Multi Agent Problem*

If $\varepsilon = \sum_i \varepsilon_i \in (0, 1)$, $\beta = \sum_i \beta_i \in (0, 1)$ and given \mathcal{S} , then

$$\mathbb{P}^{|\mathcal{S}|} \left(\mathcal{S} \in \Delta^{|\mathcal{S}|} : \mathbb{P}(\delta \in \Delta : x_S^* \notin \prod_i \mathcal{X}_i(\delta_i)) \leq \varepsilon \right) \geq 1 - \beta$$

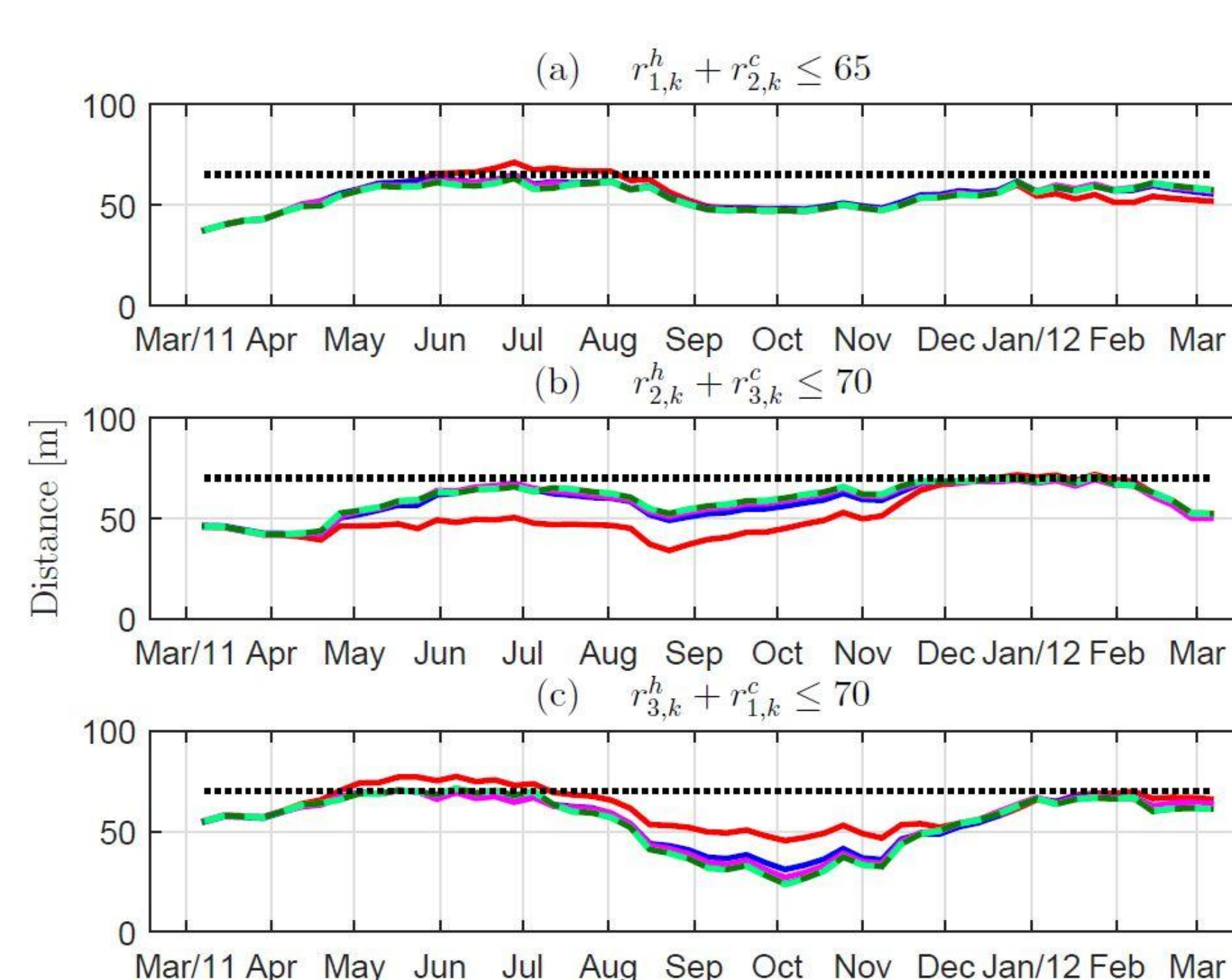
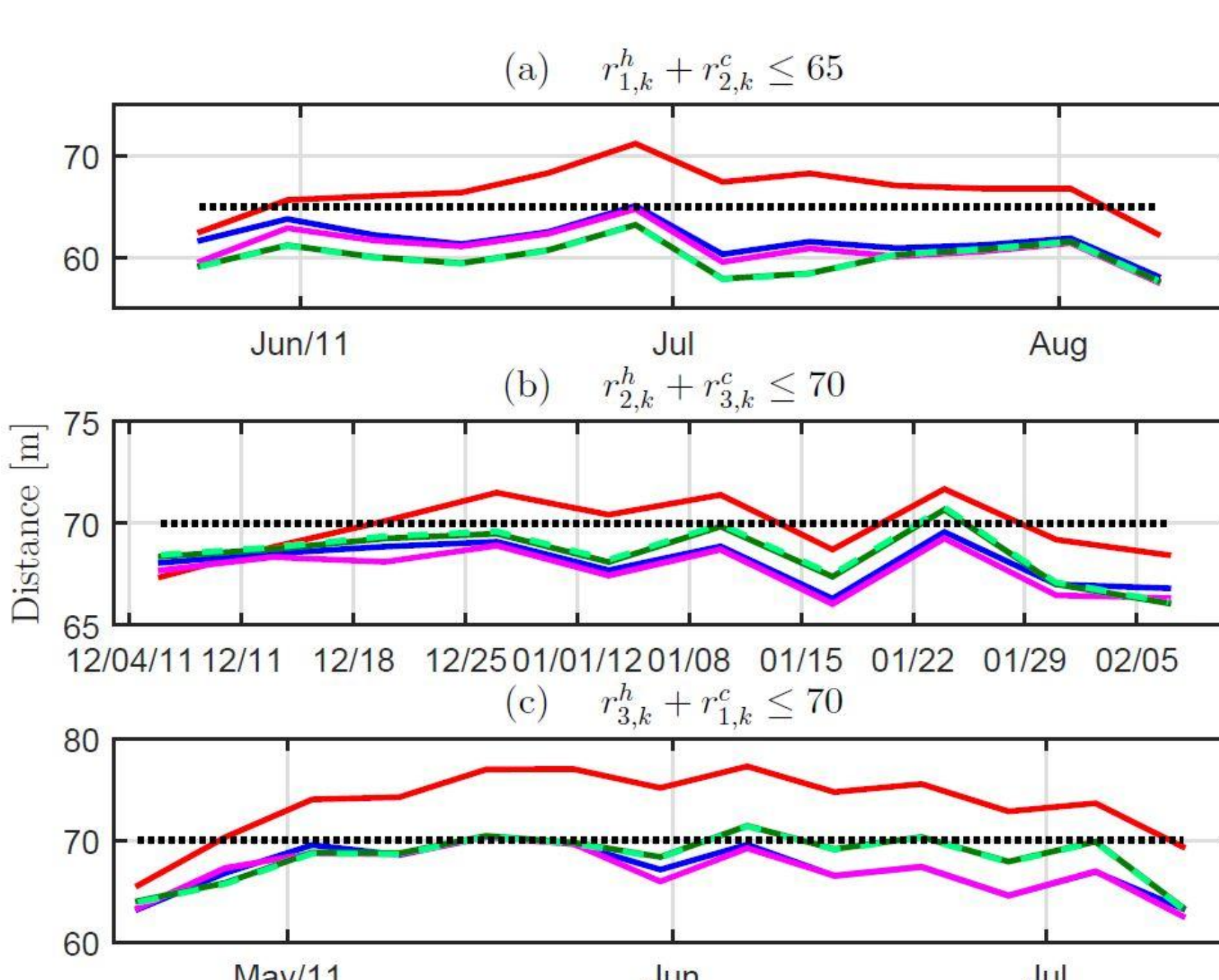
Requirements

$$\mathcal{S}_{q_i} = \left\{ q_{i,k}^{(i)} : q_{i,k}^{(i)} = C_i \delta_{i,k}^{(i)} + \sum_{j \in \mathcal{N}_i} A_{ij} x_{j,k}^{(i)}, \quad \forall \delta_{i,k}^{(i)} \in \mathcal{S}_{\delta_i}, \quad \forall x_{j,k}^{(i)} \in \mathcal{S}_{x_j} \right\}$$

Simulation Study

Case Study: three-building in Utrecht city with real parameters together with registered weather condition data from 2010-2012

- Decoupled SMPC
- Centralized SMPC
- Distributed SMPC
- DSMPC—0.85
- DSMPC—0.50



Conclusions

Remarks:

- Distributed randomized optimization to deal with private (local) uncertainty source over a network of dynamically coupled systems
- Soft communication scheme with an extension of probabilistic feasibility guarantee
- Application to energy management of smart thermal grids (STGs) with aquifer thermal energy storage (ATES) system

What comes next:

- Preserving privacy of individual agents in a network